

Dissociation Energy of the $\text{OH}\cdots\text{HF}$ Dimer

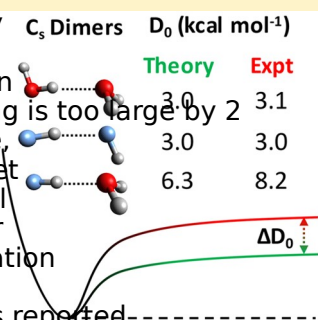
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* Supporting Information

ABSTRACT: Even though $(\text{H}_2\text{O})_2$ and $(\text{HF})_2$ are arguably the most thoroughly characterized prototypical hydrogen bonding heterodimers, $\text{OH}\cdots\text{HF}$ has received relatively little attention. Here we report that the experimental dissociation energy (D_0) of this important paradigm for heterogeneous hydrogen bonding is too large by 2 kcal/mol¹ or 30% relative to our computed value of 6.3 kcal/mol¹. For reference, computational procedures similar to those employed here to compute a large basis set CCSD(T) computations with anharmonic correction from second-order vibrational perturbation theory) provide results 0.1 kcal/mol¹ of the experimental values for $(\text{H}_2\text{O})_2$ and $(\text{HF})_2$. Near the CCSD(T) complete basis set electronic dissociation energy for $\text{OH}\cdots\text{HF}$ is ~4 kcal/mol larger than those for $(\text{H}_2\text{O})_2$ and $(\text{HF})_2$ (~9 kcal/mol for the heterogeneous dimer vs ~5 for the homogeneous dimers). Results reported herefrom symmetry-adapted perturbation theory calculations suggest that this large difference is primarily due to the induction contribution to the interaction energy.



INTRODUCTION

The dimers of O_2 and HF are among the most widely studied model systems for hydrogen bonding. The mixed dimers have received relatively little attention compared to its homogeneous counterparts $(\text{O}_2)_2$ and $(\text{HF})_2$, both of which have their own CAS registry numbers 65655-83-8 and 30664-12-3, respectively. The $(\text{H}_2\text{O})_2$ dimer is particularly well studied with energetics examined by methods to coupled cluster with single double triple and perturbative quadruple (CCSD(T))¹ excitations and with vibrational modes examined by a variety of methods including local modes.² Recent computational studies have examined heterodimers for other molecules, including CO_2 , N_2 , Ar , and HCl .³ This study examines the heterodimer of H_2O and HF . Although both HF and H_2O can readily donate a hydrogen bond, their heterodimer exhibits only one low-energy configuration in which the water molecule accepts a hydrogen bond from hydrogen fluoride, denoted here as $\text{OH}\cdots\text{HF}$.

The investigation of the $\text{OH}\cdots\text{HF}$ dimer as a prototypical hydrogen-bonded system dates to 1969 when Kollman and Allen performed the first empirical and later ab initio studies of $\text{OH}\cdots\text{HF}$. They predicted that a stable dimer would form in quantities large enough to be investigated spectroscopically. Shortly thereafter, Hancock and Green studied the deactivation of vibrationally excited gas-phase $\text{OH}\cdots\text{HF}$ by D_2O . The high deactivation rate and the similarity between the H_2O and D_2O rates led them to suggest the formation of a complex or quasicomplex between HF and H_2O , which lasted for the period of many HF vibrations, which vibrational energy transfer took place. The existence of the $\text{OH}\cdots\text{HF}$ dimer was confirmed by microwave spectroscopy in the observation of low-frequency intermolecular modes not present in the pure spectra of either monomer alone.⁴

That same year an experimental study by Thomas assigned several vibrational modes and made the first attempt at the determination of dissociation energy.¹¹ Investigations into the rotational spectrum of the $\text{OH}\cdots\text{HF}$ dimer found only a single form in the gas phase that of water as proton acceptor.⁶ However, it was not possible to discern whether the complex had C_s or C_{2v} symmetry. Subsequent investigations of the vibrational spectrum determined that the equilibrium conformation has C_s symmetry with HF and O defining the plane of symmetry (Figure 1).¹² The C_v structure is a transition state connecting two equivalent minima to form a symmetric double well potential with a low barrier on the order of 0.5 kcal/mol.¹²

Additional aspects of the $\text{H}_2\text{O}\cdots\text{HF}$ complex have been measured experimentally, including the dipole moment, plane bending potential energy function and barrier to inversion,¹² the nuclear-spin–nuclear-spin hyperfine coupling constants,¹³ a Fourier transform infrared (FTIR) spectrum in argon including evidence for inversion doubling of vibrational peaks,¹⁴ and Stark effects in the rotational spectrum.¹⁵ Force constants for hydrogen-bond stretching and out-of-plane bending potentials were found for the $\text{OH}\cdots\text{HF}$ complex and were later confirmed by repeating the experiment with the $\text{D}_2\text{O}\cdots\text{DF}$ complex.¹⁶ A second experimental determination of the dissociation energy that included the zero point vibrational energy (ZPVE) used a method based on intensities of rotational transitions near room temperature in the gas phase^{19,20} to obtain a D_0 value of 8.2 ± 0.1 kcal/mol¹. The dissociation energy from geometric equilibrium is back-

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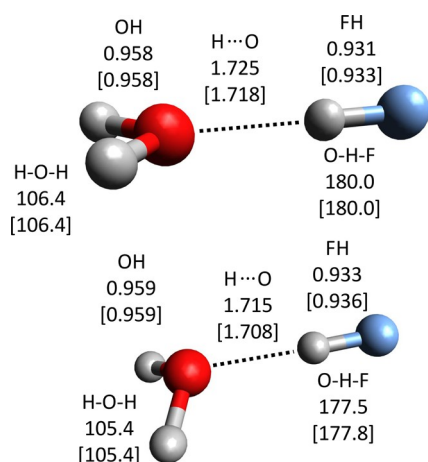


Figure 1. CCSD(T)/ha5Z optimized bond lengths and angles (deg) for the transition state (top) and global minimum (bottom) of the $\text{H}_2\text{O}\cdots\text{HF}$ dimer with corresponding MP2/ha5Z values in square brackets.

calculated based on the harmonic approximation for assigned modes and a quartic potential for the doubly excited mode, $D_e = 10.3 \pm 0.2 \text{ kcal mol}^{-1}$. These are the most current experimentally derived values for D_0 of $\text{H}_2\text{O}\cdots\text{HF}$.

For the $\text{H}_2\text{O}\cdots\text{HF}$ dimer, computational work²¹ provided assistance for the reassignment of the experimental fundamental frequency for the HF bond stretch from 3634 cm^{-1} to 3608 cm^{-1} . This reassignment invalidated the D_0 of $\text{H}_2\text{O}\cdots\text{HF}$ determined by Thomas¹⁵ that value for D_0 was computed based on the intensity of this assigned HF stretch. After reassigning this peak, Bulychov et al.²² suggested an experimental and theoretical investigation of the system was needed including additional harmonic calculations. There have also been some more recent computational investigations for the $\text{H}_2\text{O}\cdots\text{HF}$ dimer dissociation. In 1999, Halkier et al. reported $D = 8.5 \text{ kcal mol}^{-1}$ from counterpoise-corrected CCSD(T) and a two-point extrapolation to the complete basis limit (CBS) from aug-cc-pVQZ and aug-cc-pV5Z values. In 2007, Boes et al. determined the dimerization energy of dimers with the W2 method giving $D = 8.7 \text{ kcal mol}^{-1}$ for the $\text{H}_2\text{O}\cdots\text{HF}$ dimer.²⁵ Most recently, Demaison and Villars²⁶ calculated the dimerization energy at CCSD(T)/aug-cc-pV9Z as $9.0 \text{ kcal mol}^{-1}$ and noted that there was a significant difference between their results and the experimental D_0 . They speculated that the deviation was due to the difficulty in modeling the vibrational energy for the double-well potential and noted that the experimental value seemed compatible with their value. These computed values for D_0 of $\text{H}_2\text{O}\cdots\text{HF}$ are considerably larger than those found in the $(\text{H}_2\text{O})_2$ and $(\text{HF})_2$ dimers (4.6 and 5.0 kcal mol^{-1} , respectively).

The large discrepancy between the experimentally determined equilibrium dissociation energy of 10.3 kcal mol^{-1} ¹⁸ and recent theory for the $\text{H}_2\text{O}\cdots\text{HF}$ dimer is somewhat surprising given that the experimental dissociation energies for the two closely related homogeneous dimers, $(\text{H}_2\text{O})_2$ and $(\text{HF})_2$ were well described by CCSD(T) computational with quadruple- ζ quality basis sets when anharmonic effects were evaluated with second-order vibrational perturbation theory (VPT2). For $(\text{H}_2\text{O})_2$ and $(\text{HF})_2$ homogeneous complexes, computational procedure provided computed D_0 within 0.01 kcal mol^{-1} of the experimental values for the latter and 0.06 kcal mol^{-1} for the former while the differences between theoretical and experimental donor stretching frequencies were 3 cm^{-1} ($\text{H}_2\text{O})_2$ and 1 cm^{-1} for $(\text{HF})_2$.

The aforementioned experimental values for $(\text{H}_2\text{O})_2$ and $(\text{HF})_2$ were determined by vibrational dissociation (VPD) method. Other examples exist in the literature where D_0 or experimentally inferred D_0 values from VPDs of similar weakly bound complexes are in excellent agreement with modern theoretical methods, for example, $\text{H}_2\text{O}\cdots\text{HCl}$ ^{31,32} and $\text{N}_2\cdots\text{HF}$.^{33,34} When only harmonic ZPVEs were used, moderate agreement between theory (CCSD(T) and MP2 ZPVE) and experiment (various molecular beam techniques) was found for D_0 values for 10 hydrogen-bonded complexes, aromatic chromophores, and small molecules. Reasonable agreement has also been found between theoretical and experimental VPD fragmentation patterns for CCH complexes with HCl , HF , and OH radicals.³⁶

D_0 values for the small-molecule trimers $(\text{H}_2\text{O})_3$ and $(\text{HCl})_3$ determined by VPD also have good agreement with modern computational techniques.^{37,38} For the $(\text{HF})_2$ and $(\text{HCl})_2$ dimers, a gas-phase equilibrium method based on intensities of vibrational transitions³⁹ provided measurements in line with VPD results, although VPD results had smaller error bars. In contrast, the most recent experimental D_0 of $\text{H}_2\text{O}\cdots\text{HF}$ was measured using a gas-phase equilibrium technique based on absolute intensities of rotational transitions.^{18,20} For the similar $\text{HCN}\cdots\text{HF}$ dimer, D_0 values determined by absolute intensities of rotational transitions¹⁹ or by relative FTIR intensities⁴² have been later found to be significantly different from those given by more reliable VPD techniques.⁴³

To resolve the aforementioned discrepancy between experimentally and theoretically derived values of D_0 of $\text{H}_2\text{O}\cdots\text{HF}$, the present study determines an accurate zero-point corrected dissociation energy as well as fundamental vibrational frequencies using similar methods to those that were successful for $(\text{H}_2\text{O})_2$ and $(\text{HF})_2$.²⁹ These results can be directly compared with future experiments to help resolve this discrepancy. Although several groups have reported values computed by high-level methods^{24–26} and another group has computed an anharmonically corrected HF stretching frequency,²¹ this work is the first to report a fully theoretical calculation of D_0 for the dissociation of $\text{H}_2\text{O}\cdots\text{HF}$ dimer with ZPVE modeled by VPT2 with correlated ab initio electronic structure methods and large correlation consistent basis sets.

COMPUTATIONAL DETAILS

The CFOUR package⁴⁴ was used to perform all of the coupled cluster computations in this study with single and perturbative triple excitations (CCSD(T)) method,^{45,46} where a second-order Møller–Plesset perturbation theory (MP2)⁴⁷ calculations were performed with CFOUR as a Gaussian⁴⁸ MP2 and CCSD(T) geometry optimizations and harmonic frequency calculations were performed using analytic gradients and Hessians with mixed basis sets using Dunning's correlation consistent basis sets^{49,50} cc-pVXZ on hydrogen atoms and the corresponding augmented with diffuse functions (aug-cc-pVXZ) on heavy (non-hydrogen) atoms with $X = \text{T, Q, 5}$ (abbreviated as haXZ). Additional basis sets aug-cc-pVXZ (with $X = 5-6$) abbreviated as aXZ. The subset of data obtained with the larger aXZ basis sets is tabulated in the Supporting Information and the results are

Table 1 Harmonic Vibrational Frequencies (in cm^{-1}) and ZPVEs (in kcal mol^{-1}) for the C_s Form of the $\text{H}_2\text{O}\cdots\text{HF}$ Heterogeneous Dimer as well as the Corresponding Anharmonic Corrections and Estimates from VPT2

mode	harmonic		Δ VPT2 correction				VPT2
	MP2	CCSD(T)	MP2	MP2	MP2	CCSD(T)	anharmonic estimate
	ha5Z	ha5Z	haTZ	haQZ	ha5Z	haTZ	
1	223	222	−46	−51	−53	−46	169
2	245	242	−34	−34	−33	−39	209
3	264	263	−79	−78	−79	−80	184
4	712	704	−105	−104	−103	−110	601
5	837	827	−113	−112	−111	−117	716
6	1634	1651	−54	−46	−59	−46	1592
7	3736	3782	−139	−145	−146	−138	3636
8	3835	3833	−167	−169	−170	−169	3663
9	3953	3936	−178	−180	−181	−183	3755
ZPVE	22.07	22.10	−0.50	−0.50	−0.51	−0.52	21.60

^aCCSD(T)/ha5Z harmonic values with MP2/ha5Z Δ VPT2 corrections.

very similar to those from the haXZ basis. In addition, second-order vibrational perturbation theory (VPT2)^{51–54} analyses were performed with CFOUR to estimate anharmonic effects for the minimum-energy structures of H_2F and H_2O monomers and $\text{OH}\cdots\text{HF}$ dimer. Force constants needed for the VPT2 were calculated numerically from finite difference analytic second derivatives.⁵⁵ These anharmonic frequency calculations were performed with basis up to haTZ for CCSD(T) and ha5Z for MP2. In all cases, the frozen-core approximation was used, and spherical harmonic functions (5d,7f) were used instead of Cartesian A11 Cartesian forces associated with optimized structures have been converged to less than 1.0 Hartree Bohr for structures optimized by CFOUR and less than 1.0 Hartree Bohr for structures optimized by Gaussian 09.

The use of finite basis sets in the computation of dissociation or interaction energies via the supermolecular method introduces an inconsistency commonly referred to as basis set superposition error (BSSE).^{56,57} The effects of this inconsistency were assessed through the application of the counterpoise (CP) procedure for dimers.^{58,59}

RESULTS AND DISCUSSION

Optimized Structures. On the basis of the rotational spectrum of the dimer, a single form of the dimer is the gas phase. We find the same global minimum with HF as the hydrogen-bond donor and another minimum with HF as the hydrogen-bond acceptor at lower levels of theory, such as RHF/STO-3G, but optimizations from that geometry collapse to the global minimum with larger basis sets and post-Hartree–Fock methods. Therefore, only the complex with HF as hydrogen-bond donor is investigated here. The $\text{H}_2\text{O}\cdots\text{HF}$ dimer can move from the C_s global minimum (Figure 1, bottom) to a symmetry-equivalent minimum by traveling through a planar transition state (Figure 1).

Selected MP2 and CCSD(T) optimized geometrical parameters obtained with the ha5Z basis set for both stationary points are provided in Figure 1. The MP2 and CCSD(T) values are very similar. Even the differences in the intermolecular parameters do not exceed 0.007 Å and 0.16° deviations between the haQZ and ha5Z results are even smaller. This suggests the optimized structures are converged. More complete list of parameters is tabulated in the Supporting

Information along with the corresponding Cartesian coordinates.

Vibrational Frequencies of the Global Minimum. The MP2 and CCSD(T) harmonic vibrational frequencies associated with both structures are also reported in the Supporting Information. The basis set convergence of the harmonic vibrational frequencies for $\text{OH}\cdots\text{HF}$ is very similar to that observed for the $(\text{HF})_2$ and $(\text{H}_2\text{O})_2$ homogeneous dimers. The present study also reveals that haQZ is the smallest basis set in the series that consistently provides MP2 harmonic vibrational frequencies within a few inverse centimeters of the CBS limit values regardless of whether the counterpoise procedure is applied or not (average absolute deviation of 4 cm^{-1} for MP2/haQZ harmonic frequencies give a maximum deviation from CBS values of 12 cm^{-1} without counterpoise correction and 12 cm^{-1} with counterpoise correction).

Reminiscent of the behavior observed for the homogeneous $(\text{HF})_2$ and $(\text{H}_2\text{O})_2$ dimers,²⁹ the MP2/ha5Z and CCSD(T)/ha5Z harmonic vibrational frequencies in the leftmost column of data in Table 1 are quite similar for the low-energy intermolecular modes (within 10 cm^{-1}), whereas the deviations are somewhat larger for the stretching modes, reaching 46 cm^{-1} for the intramolecular modes. Consequently, the harmonic ZPVEs of the C_s minimum from MP2/ha5Z and CCSD(T)/ha5Z frequency computations are virtually identical (22.07 and 22.10 kcal mol^{-1}). The harmonic frequencies for the C_s transition state exhibit the same behavior, the magnitude of the difference is 39 cm^{-1} for the HF stretching mode and less than 10 cm^{-1} for the imaginary mode.

The C_s minimum and four different sets of anharmonic corrections from VPT2 computations (Δ VPT2) are also listed in Table 1. The MP2/haTZ and CCSD(T)/haTZ Δ VPT2 values never deviate from each other by more than 8 cm^{-1} . As a result, the corresponding anharmonic corrections to the ZPVE differ by less than 0.02 kcal mol^{-1} . Consequently, the MP2/ha5Z anharmonic corrections are used as a proxy for the CCSD(T)/ha5Z values, thereby avoiding numerous demanding analytic CCSD(T) Hessian computations. The VPT2 procedure, including some at reduced symmetry, the fundamental frequencies and anharmonic ZPVE reported in the last column of Table 1 were obtained by combining the harmonic CCSD(T)/ha5Z values with the MP2/ha5Z Δ VPT2 values.

Table 2. Dissociation Energies (D_0) and Various ZPVE Corrections (in kcal/mol) for the $\text{H}_2\text{O}\cdots\text{HF}$ Heterogeneous Dimer

	D_e	harmonic		VPT2		
		δZPVE	D_0	δanharm	δZPVE	D_0
MP2/haTZ	8.83	−2.70	6.12	+0.24	−2.46	6.37
MP2/haQZ	8.75	−2.67	6.08	+0.24	−2.42	6.32
MP2/ha5Z	8.71	−2.65	6.07	+0.24	−2.40	6.31
MP2/ha5Z(CP)	8.58					
CCSD(T)/haTZ	8.81	−2.75	6.05	+0.25	−2.50	6.31
CCSD(T)/haQZ	8.74	−2.71	6.03	[+0.24]	[−2.47]	[6.27]
CCSD(T)/ha5Z	8.70	−2.70	6.01	[+0.24]	[−2.45]	[6.25]
CCSD(T)/ha5Z(CP)	8.61					
CCSD(T)/CBS(CP)	8.51		ref 24 (aQZ/a5Z extrapolation)			
W2	8.69		ref 25			
CCSD(T)/a5Z	8.97		ref 26			
experiment	10.25 ± 0.19		ref 18		8.20 ± 0.07	

^aCP procedure only applied to VPT2 anharmonic shift to ZPVE (δanharm) from corresponding MP2/haXZ computations.

The HF stretch associated with the donation of the hydrogen bond has been the most thoroughly scrutinized of due to inversion doubling and multiple environments. HF vibrational modes both theoretically and experimentally. The experimental barrier for the $\text{H}_2\text{O}\cdots\text{HF}$ inversion was determined to be $126 \pm 70 \text{ cm}^{-1}$ with the associated reassignment of 3634 cm^{-1} and its change on complexation was a vibrational mode of $64 \pm 10 \text{ cm}^{-1}$. Each level of theory found to be $\sim 332 \text{ cm}^{-1}$ in 1999, Silvi et al. calculated the employed in this study gives an electronic barrier height that shift in HF stretch on complexation by MP3/6-311++G(2d,2p) smaller than the fundamental frequency of the inversion with and without CP correction based on a fourth-order mode. For example, the CCSD(T)/haTZ level barrier to polynomial fit of energy points without CP correction the inversion was 133 cm^{-1} and the associated VPT2 frequency shift on complexation ($\sim 357 \text{ cm}^{-1}$) was close to the was 178 cm^{-1} . Regardless of whether inversion doubling occurs experimentally value ($\sim 354 \text{ cm}^{-1}$) based on the mis-assignment in the $\text{H}_2\text{O}\cdots\text{HF}$ complex or not, the experimental data and our peak. The same procedure with counterpoise correction computations results indicate that the overall effect on the shift ($\sim 332 \text{ cm}^{-1}$) equivalent to that for the reassigned ZPVE contribution to the dissociation energy will

Our fully anharmonic HF stretching frequency of 3636 cm^{-1} . Dissociation Energy Several computational determinations of D_0 and D_e are shown in Table 2 along with the MP2/ha5Z aligns well (within 2%) with the reassigned HF experimental values. Recent high-level theoretical values for stretching mode 3634 cm^{-1} . The HF stretching frequency D_e range from ~ 8.5 to 9.0 kcal/mol and MP2 and CCSD(T) with harmonic CCSD(T)/ha5Z and VPT2 vibrational D_e values obtained with the ha5Z basis set of 8.71 and 8.70 corrections from MP2/haQZ is also within (Table 1). mot^{-1} , respectively, fall in the middle of this range. The CP

The only resonance between modes reported by the VPT2 procedure only decreases by $\sim 0.1 \text{ kcal/mol}^{-1}$, which computations CFOUR at the MP2/haTZ, MP2/haQZ, suggests the results are close to the CBS limit BSSE MP2/ha5Z or CCSD(T)/haTZ levels was between the first must vanish by definition. Also noteworthy that for a given overtone of the out-of-plane HF libration (mode 5) and basis set the MP2 and CCSD(T) D_e differ by no more H_2O bending fundamental (mode 6), which have CCSD(T)/ha5Z harmonic frequencies at 827 and 1654 cm^{-1} . For further insight into the exceptionally large of the That overtone also had the most significant IR intensity of dimer relative to the (H_2O) and (H_2O)₂ dimers, high-overtones and combination bands computed with uplevel symmetry-adapted perturbation (SAPT) calculations of three vibrational modes ranging from 66 to 147 kcal/mol were performed for the systems to compare depending on the method and basis set employed for the VPT2 energy contributions in electrostatic, computational. Only five other overtones and combination exchange induction and dispersion contributions with SAPT2 bands had VPT2 intensities of at least 10 kmol^{-1} in this group + 3(CCD) δ_{MP2} using the haQZ basis set in the Psi4 software consists of the overtones 4(2,2) and 5(2) along with two package. Both the attractive electrostatic and repulsive combination bands 1(1) + 3(1) and 1(1) where the exchange components much larger than the mixed $\text{H}_2\text{O}\cdots$ integer in parentheses denote the number of vibrational HF dimer increasing in magnitude by $\sim 6 \text{ kcal/mol}$ and quanta for that mode. These six VPT2 frequencies and IR making contributions of opposite signs to the total intensities can be found in the Supporting Information energy. However, the increased stabilization is due to the

Inversion Barrier The study of the $\text{H}_2\text{O}\cdots\text{HF}$ dimers complicated by the low inversion barrier between the $\sim 100 \text{ kcal/mol}^{-1}$ yield an interaction energy with a forms Symmetric double-well potentials with small barriers magnitude more than 4 kcal/mol larger than that for either have a fine structure, where all lines are doubled for homodimers. See the Supporting Information for the SAPT energies below the barrier as demonstrated for the case energy components in each dimer.) of NH_3 inversion doubling. Such splitting may be present to determine an accurate $\text{H}_2\text{O}\cdots\text{HF}$, harmonic and in the $\text{H}_2\text{O}\cdots\text{HF}$ dimer the vibrational spectrum of the HF anharmonic ZPVE corrections were calculated with basis librational modes for the $\text{H}_2\text{O}\cdots\text{HF}$ complex in a solid argon sets ranging from haTZ to ha5Z MP2 and CCSD(T)

levels of theory. The MP2 and CCSD(T) harmonic ZPVE corrections to D_0 are the second column of data in Table 2 and are quite similar to ZPVE values within $0.05 \text{ kcal mol}^{-1}$ of each other for a given basis set. Of course, this is a consequence of the trend in vibrational frequencies already discussed. The harmonic δZPVE corrections decrease by $2.0 \text{ kcal mol}^{-1}$ to yield MP2/ha5Z and CCSD(T)/ha5Z harmonic values of 6.07 and $6.01 \text{ kcal mol}^{-1}$, respectively.

Intramonomer and intermonomer modes of the H₂O...HF complex have opposite contributions to δZPVE . The intramonomer harmonic vibrational frequencies shift to lower energy upon complexation, which increases the computed dissociation energy D_0 by $\sim 0.5 \text{ kcal mol}^{-1}$. Conversely, the new intermonomer harmonic vibrational frequencies have the opposite effect and appreciably larger magnitude (by roughly a factor of 2) than the intramonomer frequencies for O_2 , H_2O , $\text{H}_2\text{O}\cdots\text{HF}$, $(\text{HF})_2$, and their monomers. The Supporting Information can be found in the Supporting Information.

Anharmonicity (δanharm in Table 2) slightly attenuates the effect of the ZPVE on the dissociation energy. VPT2 computations indicate that these anharmonic effects decrease the magnitude of δZPVE by $\sim 0.2 \text{ kcal mol}^{-1}$, thereby slightly increasing D_0 relative to the harmonic estimates. Notably, the MP2/haQZ and MP2/ha5Z anharmonic correction (δanharm) were applied to the corresponding CCSD(T) harmonic δZPVE values to estimate the VPT2 δZPVE results. At the CCSD(T)/haQZ and CCSD(T)/ha5Z levels of theory, the MP2 and CCSD(T) VPT2 values remain remarkably consistent at $6.31 \text{ kcal mol}^{-1}$ for MP2/ha5Z and $6.25 \text{ kcal mol}^{-1}$ for CCSD(T)/ha5Z.

These anharmonic values differ significantly from the most recent experimental determination of $6.20 \pm 0.07 \text{ kcal mol}^{-1}$.¹⁸ Although inversion doubling could occur (vide supra), the related intermonomer mode is low in energy and thus contributes only a small amount to the overall ZPVE contribution to D_0 . $(\text{HF})_2$ also has a similar double-well potential for the analogous mode. CCSD(T)/haQZ with VPT2 was found to be a good model for the $\text{H}_2\text{O}\cdots\text{HF}$ dimer, within $0.01 \text{ kcal mol}^{-1}$ of the experimental value. According to our calculations, the total anharmonic ZPVE correction to obtain D_0 from D_e is $\sim 2.5 \text{ kcal mol}^{-1}$ for $\text{H}_2\text{O}\cdots\text{HF}$ (Table 2). This correction is substantially similar to the $2.1 \text{ kcal mol}^{-1}$ difference between D_0 and D_e given by Legon et al.¹⁸ For comparison, previous work has found a ZPVE correction of $1.6 \text{ kcal mol}^{-1}$ for $(\text{HF})_2$ and $1.9 \text{ kcal mol}^{-1}$ for $(\text{H}_2\text{O})_2$. As such, the large discrepancy between the experimental and the values computed here cannot be attributed to the challenges of reliably modeling the ZPVE correction in this system.

CONCLUSIONS

The energies and frequencies of the dimer have been calculated with the MP2 and CCSD(T) methods in conjunction with large correlation consistent basis sets. CCSD(T)/ha5Z computations yield $D_0 = 8.70 \text{ kcal mol}^{-1}$ and $D_0 = 6.25 \text{ kcal mol}^{-1}$ after including an anharmonic ZPVE correction from an MP2/ha5Z VPT2 analysis. Results from this level of theory provide fundamental energies and dissociation energies appropriate for comparison with experimental values. On the basis of the very accurate descriptions of these quantities for $(\text{H}_2\text{O})_2$ and $(\text{HF})_2$ by analogous theoretical treatments, the $2.0 \text{ kcal mol}^{-1}$ discrepancy between our

computed D_0 and the experimental value of $6.2 \text{ kcal mol}^{-1}$ is unexpected for this very important prototype for heterogeneous hydrogen bonding. Although the heterodimer is expected to be more stable than either homodimer, our computations show that the heterodimer is approximately twice as large as that for either homodimer (6.3 vs $\sim 3.0 \text{ kcal mol}^{-1}$). That ratio approaches 3 with the current experimental value for $\text{H}_2\text{O}\cdots\text{HF}$ ($8.2 \text{ kcal mol}^{-1}$). It is suggested that the experimental value of the dissociation energy be redetermined for the heterodimer, because it is 30% larger than our best estimate reported in this study. A SAPT analysis suggests that induction is primarily responsible for the significant increase in D_0 for $\text{H}_2\text{O}\cdots\text{HF}$ ($\sim 8.7 \text{ kcal mol}^{-1}$) relative to the values for $(\text{H}_2\text{O})_2$ ($\sim 5.0 \text{ kcal mol}^{-1}$) and $(\text{HF})_2$ ($\sim 4.6 \text{ kcal mol}^{-1}$, respectively).

ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.jpca.8b03397. Cartesian coordinates, harmonic and anharmonic frequencies, and intensities analysis of harmonic contributions to ZPVE, SAPT energy components, citations for CFOUR, Gaussian 09, and Psi4 (PDF)

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Notes

The authors declare no competing financial interest.

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